Suppose that $A$ is a $2 \times 2$ matrix with entries in a field.

Prove: If $A^2 \neq O$, then $0 \leq n \Rightarrow A^n \neq O$. 