

Answer **ANY TWO** of the following three questions:

1. Prove that the language $\{0^n1^n: n \geq 0\}$ over $\Sigma = \{0,1\}$ is **not** regular.
2. Show that the following context-free grammar is ambiguous:

$S \rightarrow S0S$

$S \rightarrow S1S$

$S \rightarrow A$

$A \rightarrow 0$

3. Answer each of the following questions with **YES** or **NO** to indicate whether the **conclusion is always true**. If you do not know the answer, *do not guess*.
Scoring: +2 points for correct answers; 0 points for no answers; -1 point for wrong answers

- a. If $A \leq B$ and B is not decidable, **then A is not decidable**.
- b. If $A \preceq B$ and A is NP-Complete, **then B is NP-hard**.
- c. If $A \leq B$ and B is co-acceptable, **then A is acceptable**.
- d. If $A \preceq B$ and A is NP-Complete, **then B is decidable**.
- e. If $A \leq B$ and B is NP-Complete, **then A is NP-Complete**.
- f. If $A \preceq B$ and B is in NP, **then A is co-acceptable**.
- g. If $A \leq B$ and B is decidable, **then A is decidable**.
- h. If $A \preceq B$ and B is NP-Complete, **then A is in NP**.
- i. If $A \leq B$ and B is in P, **then A is acceptable**.
- j. If $A \preceq B$ and B is in NP, **then A is in NP**.